

# §11-1 Projectile Motion (neglecting air resistance)

## Horizontally

- Velocity is constant:  $v_h = \frac{\Delta d_h}{\Delta t}$

## Vertically

- constant acceleration due to gravity: ( $a = -9.8 \text{ m/s}^2$ )

$$v_{\text{ave}} = \frac{\Delta d_v}{\Delta t} \quad \left( v_{\text{ave}} = \frac{v_1 + v_2}{2} \right)$$

$$a = \frac{\Delta v}{\Delta t}$$

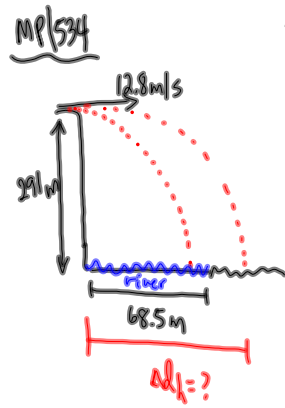
Maybe useful:

$$\Delta d = v_1 t + \frac{1}{2} a t^2$$

$$\Delta d = v_2 t - \frac{1}{2} a t^2$$

$$\underline{v_2^2} = \underline{v_1^2} + \underline{2a(\Delta d)} \quad \leftarrow \text{vertical}$$

vertical      vertical



Time for the rock to fall ... look at the vertical motion:

constant acceleration  
 $a = -9.81 \text{ m/s}^2$   
 $\Delta d = -291 \text{ m}$   
 $v_i = 0$   
 $\Delta t = ?$

$$\Delta d = v_i \Delta t + \frac{1}{2} a (\Delta t)^2$$

$$\Delta d = \frac{1}{2} a (\Delta t)^2$$

$$\frac{2\Delta d}{a} = (\Delta t)^2$$

$$\Delta t = \sqrt{\frac{2(-291 \text{ m})}{-9.81 \text{ m/s}^2}}$$

$$\Delta t = 7.70 \text{ s}$$

Horizontally  
constant velocity

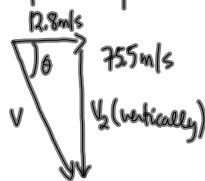
$$v = \frac{\Delta d}{\Delta t}$$

$$\Delta d = (12.8 \text{ m/s})(7.70 \text{ s})$$

$$\Delta d = 98.6 \text{ m}$$

a) Since  $98.6 \text{ m} > 68.5 \text{ m}$ , the rock lands on the other side of the river.

b) Velocity at impact?



$$a = \frac{\Delta v}{\Delta t} \leftarrow \text{for vertical velocity}$$

$$a = \frac{v_2 - v_1}{\Delta t}$$

$$v_2 = v_1 + a \Delta t$$

$$v_2 = (-9.81 \text{ m/s}^2)(7.70 \text{ s})$$

$$v_2 = 75.5 \text{ m/s}$$

$$c^2 = a^2 + b^2$$

$$v^2 = (12.8)^2 + (75.5)^2$$

$$v = 76.6 \text{ m/s}$$

$$\tan \theta = \frac{75.5 \text{ m/s}}{12.8 \text{ m/s}}$$

$$\theta = 80.4^\circ$$

The velocity at impact is:  $76.6 \text{ m/s}$  [ $80.4^\circ$  below the horizontal]

PP|536-537